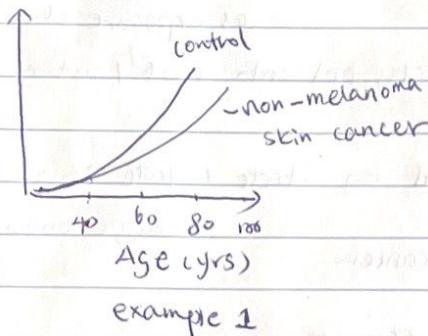
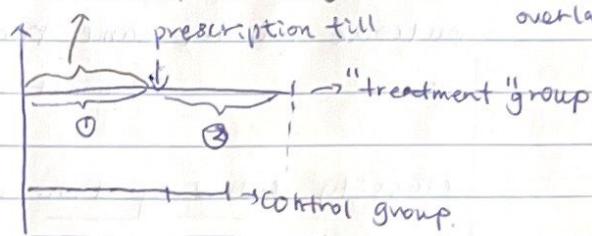


immortal time bias



example 1

observing exposure & outcome at the same time
(in ①, the exposure start & outcome start)
immortal time bias
status are overlapping)



example 2

① selection bias in the skin cancer group.

↳ to be selected as the "skin cancer" group, you need to be alive to be diagnosed as skin cancer patient. $P(\text{skin cancer} | \text{alive})$ which introduces selection bias.

↳ for control group, no restriction

↳ so not surprising to observe higher survival in skin cancer group

② don't condition on future event / survival behavior / be immortal

* ③ tricks: when classifying ppl into treat/control groups. do not use things that change over time (e.g. skin cancer diagnosis). rather, use variable that does not change over time to stratify ppl into treat/control group.

wrong ← in example 2, if we see in the "treatment" group. in ①, ppl are not exposed, in ② time interval, 100% are exposed. so ppl in the "treatment" group are ~~not~~ both treated & untreated.

correct ① by design

analysis use ~~variable~~ variable

that doesn't change over time to stratify

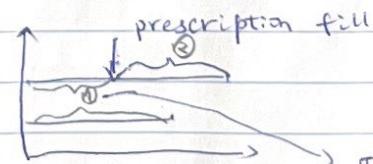
treat and control.

e.g. treat: skin cancer diagnosis before age 40.

control: no skin cancer before age 40.

follow up pts from age 40.

② by analysis.



① immortal time

being classified into the control group. using person-time

KM not appropriate when we're observing exposure and outcome at the same time
 as exposure changes over time
 so cannot stratify ppl into treat/control if ↑

classify follow up time based on state (State is something that changes over time)

↳ follow-up time before skin cancer

↳ follow-up time after skin cancer

cannot classify ppl into specific group.

Time-dependent covariates

Counting process:

value of covariate

$$Z_i(t) = \{Z_i(u); 0 \leq u \leq t\}$$

↳ whole history before time t
 capital Z

↳ covariate history of i till time t .

$$\lambda_i(t) = P[t \leq \tilde{T}_i < t+dt | Z_i(t), \tilde{T}_i > t]$$

Simplified version: if we assume that the hazard function depends only on the current value of the covariate, rather than the cumulative history:

$$\lambda_i(t) = P[t \leq \tilde{T}_i < t+dt | z_i(t), \tilde{T}_i > t]$$

↳ small ϵ , current time